Image Compression using Quadrature Mirror Filter Bank based IndBp Mother Wavelet

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Abstract*—Development in today Digital Technology has increased the use of image in practically all the application. The extensive use of these Images have raised the need of image compression. The image compression using new mother wavelet involved design of low pass FIR filter followed by design quadrature mirror filters which leads to the design of our perfect reconstruction mother wavelet. The results shows better quality of image even after compression.*

Keywords—FIR Low Pass Filter, Quadrature Mirror Filter, Compression Ratio, Transform Technique, Mother Wavelet

I. INTRODUCTION

Image is one of the most important media of information contributing to multimedia. This is all the more true in modern era. This information has become one of the most value of the assets. The unprocessed image heavily consumes very important resources of the system. Uncompressed Image requires large memory to store the images and large bandwidth to transmit the image data .While the advancement of the computer storage technology continues at the rapid rate the means for reducing the storage requirements of images is still needed in most of the situations and hence it is highly desirable that the image be processed so that efficient storage representation and transmission of it can be worked out. The process involved image compression methods for digital images. Image compression have been the subject of research over the past decades. The image compression mechanism that is proposed by joint photographic expert group (JPEG) is today's still image lossy compression standard and it is used for natural images. It combines block for implementation using DWT quantization technique and then coding technique[1].

Although these methods are efficient even if lower average bit rate is employed the block noise appears in the resulting image.

Advances in Wavelets Transform and Quantization methods have produced algorithms capable of surpassing image compression Standards,like the JPEG Joint Photographic Expert Group algorithms. The recent growth of data intensive multimedia based application have not only sustained the need for more efficient way to encode the signal and images but also have made compression of such signals central to storage and communication technology[1].

Recently based on theory of wavelets or analysis has attracted much attention in signal processing .It has been successfully applied in many applications such as transient signal analysis, images analysis, communication system and other signal processing applications. It is not a new theory in the sense that many of the ideas and techniques involved in wavelets were (sub band coding,[2] quadrature mirror filters etc) to developed independently in various signal processing applications and has been known for sometimes. Now what is new is the development of recent results is the mathematical foundation of wavelets that provides a unified framework for the subject. There are opportunity for further development of both the mathematical understanding of wavelets and a wide range of application in science and engineering.

Like Fourier analysis, wavelet analysis deals with expansion of function in terms of set of basic functions. Unlike Fourier analysis, wavelet analysis expand functions not in terms of trigonometry polynomial but in terms of wavelets which are generated in the form of translations and dilation of a fixed function called the mother wavelets.

The wavelets [2] obtained in this way have special scaling properties they are localized in time and frequency, permitting a closer connection between the functions being represented and their coefficient. Greater numerical stability in reconstruction and manipulation is ensures [3].

The Development of wavelets analysis can be considered an outgrowth of the little wood Paley theory (In 1931 Published) which sought a new [4] approach to answer some of these difficulties. It is again the unifying framework made possible by recent results in wavelets theory related to problem of harmonic analysis [2].

There have been independent development in the analysis of non-stationary signals specifically in the form of the short term Fourier Transform [5] was first published in 1946. A major advanced in wavelets theory was the discovery of smooth mother wavelets whose set of discrete translation and dilation forms an orthonormal basis for space L which is the set of all functions f that has bounded energy.

This is a main difference from the Gabor Transform, in the Gabor case, no orthonormal basis can be generated from smooth wavelets. Thus the unifying framework brought about a better understanding and a new approach that overcomes the difficulties in the short term Fourier Transform methods.

The JPEG 2000 Standard employs wavelets for compression due to its merits in terms of scalability localization and energy concentration. It also provide the user with many options to choose to achieve further compression. JPEG 2000 suffer from blurring artifacts and ringing artifacts. This paper presents the results of image compression for different images for a mother wavelet. It is concluded that using QMFPR mother wavelet the quality of image is perfect after image compression.

II. IMAGE COMPRESSION

Image compression is a procedure used to reduce the amount of data used to represents a digital image. The reductions in the data reduces the number of bits required to store or transmit the image over digital media.

Images compression is also of two types in which

- Lossless
- Lossy
- Lossless: In which the reconstruction image is exact replica of the original image. The reconstructed image after the compression is exactly identical to the original image then the compression is known as lossless compression[9].
- Lossy: where the reconstructed image is not an exact replica of the original image then the compression is known as lossy- compression. In lossy compression, there is always some loss. The extend of compression is more in lossy compression technique compared to lossless compression technique but the reconstructed images is superior in lossless compression.

A. Compression Ratio

Compression ratio is the ratio of number of bits required to represent original image to the number of bits required to represent compressed images.

Compression ratio=size of original image/ compressed image size

B. Mean Square Error (MSE)

Mean Square error is the cumulative squared error between the compressed images & the original images

$$MSE = \frac{1}{MN}\sum_{Y=1}^{M}\sum_{X=1}^{N}[I(x,y) - I_1(x,y)]^2$$

C. Peak Signal to Noise Ratio(PSNR)

Peak signal to noise ratio is the ratio of maximum power of the signal and the power of Noise signal.

$$PSNR = 20 * log_{10}(255/\sqrt{MSE})$$

III. DESIGN OF QMF BANK USING FIR LOW PASS FILTERS

The image compression needs the design of a FIR low pass filter and it needs to specify pass band, stop band, and transition band when designing a frequency selective filters.

In pass band (s) frequency are passed un-attenuated. In stop band (s) frequencies are completely attenuated. Transition band frequencies are lying between the passband(s) and stopband (s). In practical, the magnitude is not necessary to be constant in the passband of a filter. A small amount of ripple is usually allowed in the passband .Similarly, the filter response need not to be zero in the stopband. A small non zero value is also tolerable in the stopband[10].

To design FIR low pass filter many different methods were used but this paper uses design of low pass filter using PM algorithms which has high calculation accuracy.

The coefficients of linear phase FIR filter of length M=16 which has a symmetric unit sample response and a frequency response that satisfy the following conditions are determined

$$G(k) = (-1)^k H_r\left(\frac{2\pi k}{M}\right), \qquad G(k) = -G(M-k) \quad (1)$$

$$h(n) = \frac{1}{M}\left\{G(0) + 2\sum_{k=1}^{U} G(k)\cos\frac{2\pi k}{M}\left(n+\frac{1}{2}\right)\right\} \quad (2)$$

$$U = \begin{cases} \frac{M-1}{2} & M \text{ odd} \\ \frac{M}{2}-1 & M \text{ even} \end{cases}$$

$$G(k) = (-1)^k H_r\left(\frac{2\pi k}{15}\right), \qquad k = 0,1 \ldots..8 \quad (3)$$

The PM algorithms are run 100 times and the best and average results are recorded. The best optimized filters[5] co-efficient obtained for the desired low pass filter. The various performance parameters of the designed filters are recorded to show its effectiveness. The designed linear phase LP FIR filter provides maximum stopband attenuation as high as which is greater than that achieved by other results reported in designed[6].

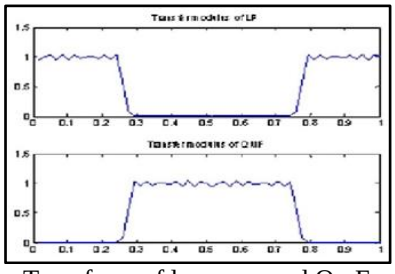
MATLAB is used to design the QMF filter. The design of synthesis and analysis of QMF filter for perfect reconstruction. Synthesized the signal exactly from its DWT. The FIR filters in the[10] filter bank must satisfy certain conditions.

Earlier it was noted that the distortion that will occur are the aliasing and images distortion. To rectify this problem, the synthesized filters must possess the power complimentary or Smith Barnwell Property.

The discrete time fourier transform of the synthesize filter used in the wavelets are g_o and g_1 respectively. The wavelets used in the DWT are either orthogonal or bio orthogonal depending on the type of DWT. The filter banks must satisfy the set of conditions. In a two channel perfect reconstruction orthogonal DWT the FIR filters used in the filter bank passes the following properties.

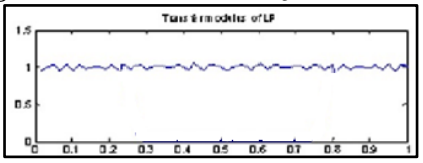
- The filters length is even.
- The filter g_0 and g_1 satisfy the power complementary condition. Similarly, the filter pairs $\{h_o(n),h_1(n)\}$,$\{h_o(n),g_1(n)\}$ and $\{g_o(n),h_1(n)\}$ satisfying the power complementary condition.
- The filter $g_o(n)$ and $h_o(n)$ are time reversed version of each other i.e$h_o(n)= g_o[-n]$
- The filter $g_0(n)$ and $h_0(n)$ are time reversed version of each other.
- The filter $h_1(n)$ and $h_o(n)$ satisfy the conditions $h_1(n)=(-1)^{n+1}h_o[L-1-n]$
- The filters $g_1(n)$ and $g_0(n)$ are time reversed and modulated version each other $g_1(n)=(-1)^n g_o[L-1-n]$
- Finally $\sum_N H_0[N]=\sum_N G_0[N]=\sqrt{2}$
- The filter $g_o[n]$ and $h_o[n]$ are low pass, while $g_1[n]$ and $h_1[n]$ are high pass

A. Design of QMF filter bank results



Transform of low pass and QmF

Fig. 1:Shows TF of LP and QMF filter bank



QmF bank condition follows power complimentary condition

Fig. 2:Shows power complimentary conditions follows equal to one

$$|H_0(z)|^2 + |H_1(z)|^2 = 1 \quad (4)$$

IV. DESIGN OF SMITH BARNWELL MOTHERWAVELET USING QMF BANK

With the help of QMF bank condition a new mother wavelet is formed it follows the power complementary condition which is having 0.5 cut off frequency.

FIR filters follows only few motherwavelets [12] they are,

- Haar mother wavelet.
- Daubechies wavelets;.dbN
- Symlet wavelets; symN
- Coiflet wavelets ; coifN
- Biorthogonal wavelets pairs Nr.Nd;Bior.Nr.Nd

A new designed Barnwell mother wavelet having some of important properties.

1) Compactly supported orthogonal
2) Symmetry, asymmetric and near symmetry.
3) Existence of ,,,,
4) Orthogonal analysis and biorthogonal analysis.
5) Exact reconstruction.
6) Arbitrary regularity and number of vanishing moments.
7) Vanishing moments for,

Due to symmetry and asymmetric property[11] the results and design of Barnwell mother wavelets provide exact reconstruction.

Procedure for Barnwell mother wavelets based images.

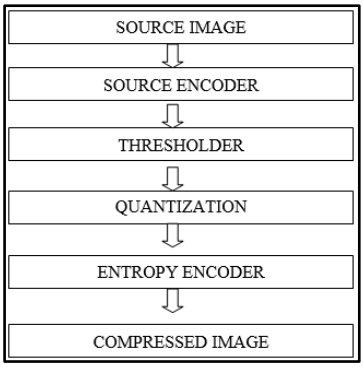


Fig. 3: Flow chart shows Image compression methods.

V. RESULTS

With the help of QMFPR mother wavelets which is formed from QMF bank filters is ready to apply to various images shows.

The perfect reconstruction of images and images compression are as follows.

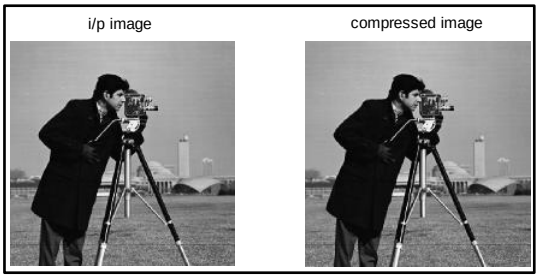


Fig.4: Shows original and compressed image.

The MSE and PSNR values verify that the compression and reconstruction of the original transmission images are better.

Images	Level	CR	PSNR	MSE
Cameraman1	1	53.8249	56.6445	0.1419
Cameraman2	5	52.9328	56.5726	0.1443

Table 1:Shows MSE, PSNR and compression ratio.

VI. CONCLUSION

Paper shows image compressions using mother wavelets. A higher compression ratio is obtained by applying QMFPR mother wavelets. Quality of images is good in terms of MSE, PSNR and further compression can be obtained by applying various coding technique on images.

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